

II. ITINERANT ELECTRON FERROMAGNET MODEL

It is the purpose of this section to present an elementary theory, unifying several existing theories, of a single band, itinerant electron FM. In particular, we shall develop a theory, appropriate for 3-d electrons, for the Curie temperature, T_c , and its pressure derivative, $\partial T_c / \partial P$; and we shall show how estimates of the effective exchange, I , times the density of states at Fermi level, $N(\epsilon_F)$, can be made from the measurements of $\partial T_c / \partial P$. The theory presented here follows quite closely the earlier work of Wohlfarth,⁹ Edwards and Wohlfarth,¹⁰ Shiga,¹³ and Wohlfarth and Bartel,¹² but includes details which have not been discussed in these earlier works.

For our model we assume that the exchange splitting is given by $nI\zeta$ where I is the effective intra-atomic exchange (accounting for the electron correlations) between the itinerant electrons, n is the number of d-electrons per atom, and ζ is the relative magnetization per electron arising from single-particle excitations. In the Stoner theory, the exchange splitting is $2k_B\theta'\zeta$ where $k_B\theta'$ is the molecular field approximation interaction; thus $k_B\theta' = 1/2 nI$. The single particle excitations are described by the Stoner equations^{9,10}

$$1/2 n(1 \pm \zeta) = \int_0^\infty f(\epsilon, \eta^\pm) N(\epsilon) d\epsilon \quad , \quad (1)$$

where

$$f(\epsilon, \eta) = \left\{ \exp [(\epsilon - \eta)/k_B T] + 1 \right\}^{-1} \quad ,$$

and

$$\eta^\pm = \mu \pm 1/2 nI\zeta \pm \mu_B H \quad .$$

Here μ is paramagnetic chemical potential, H is the applied magnetic field, and $N(\epsilon)$ is the density of states. In the limit as $T \rightarrow T_c$ such that $\zeta \rightarrow 0$ and

letting $H = 0$, we can expand the Fermi function exponentials in the expression for ζ , Eq. (1), and obtain the well known result

$$I \int_0^{\infty} N(\epsilon) \left| \frac{\partial f}{\partial \epsilon} \right|_{\substack{T=T_c \\ H=0}} d\epsilon = 1 \quad (2)$$

Within the framework of the model, Eq. (2) can be solved for T_c if $N(\epsilon)$ is known. Even if we don't know $N(\epsilon)$ we can solve Eq. (2) by use of the Sommerfeld expansion. To terms quadratic in T_c we obtain¹⁴

$$T_c^2 = T_F^2 (\bar{I} - 1) / \bar{I} \quad , \quad (3)$$

where

$$\bar{I} = IN(\epsilon_F) \quad . \quad (4)$$

Here $N(\epsilon_F)$ is the density of states per atom per spin at the paramagnetic Fermi level, and T_F is the effective degeneracy temperature defined by^{9,10}

$$T_F^2 = \left\{ \frac{\pi^2}{6} k_B^2 \left[\left(\frac{N'(\epsilon_F)}{N(\epsilon_F)} \right)^2 - \frac{N''(\epsilon_F)}{N(\epsilon_F)} \right]^{-1} \right\} \quad , \quad (5)$$

where $N^{(m)}(\epsilon_F)$ is the m -th derivative with respect to energy evaluated at ϵ_F . The expression for T_c^2 , Eq. (3), is identical to what one would obtain from the singularity in the exchange enhanced susceptibility where the F-integral of Lang and Ehrenreich¹⁵ is expanded by means of a Sommerfeld expansion. In order for the system to be FM, we have from Eq. (3) the Stoner criterion, $\bar{I} \geq 1$.

The expression for T_c^2 , Eq. (3), is general to the extent that we have not specified the origin or nature of I and we have not restricted $N(\epsilon_F)$. To find